

# Confirmation of Plazek's Slight Shoulder in the Shear Retardation Spectrum of Poly(vinyl acetate) at the Dynamic Glass Transition

S. Reissig, M. Beiner, J. Korus, K. Schröter, and E. Donth\*

Fachbereich Physik, Universität Halle, D-06099 Halle (Saale), Germany

Received March 24, 1995

Revised Manuscript Received May 24, 1995

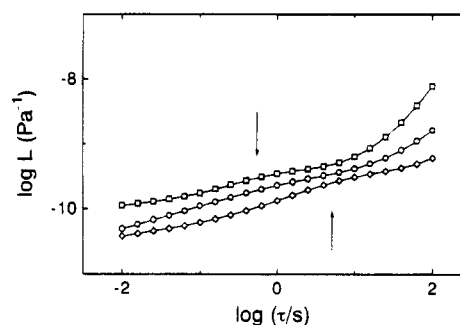
Plazek reported a slight shoulder in the shear retardation spectrum,  $L(\log \tau)$ , of poly(vinyl acetate) (PVAC)<sup>1</sup> and polypropylene (PP)<sup>2</sup> just at the same position where the shear loss modulus ( $G''(\omega)$ ) has its glass transition maximum ( $\omega\tau = 1$ ). He did not decide whether this is a real effect or "caused by experimental uncertainty"<sup>1</sup> or "by temperature-reduction errors".<sup>2</sup> On the other hand, this shoulder was assumed, in the framework of a study on the fine structure of the main transition in polymers,<sup>3,4</sup> to be a direct indicator of the "proper" glass transition manifested by the  $G''$  maximum, the dielectric loss maximum ( $\epsilon''$ ), and others. The aim of this paper is an experimental confirmation of this shoulder and its comparison with  $G''$ ,  $\epsilon''$ , and heat spectroscopy data.

**Experimental Section.** A carefully dried PVAC sample ( $M_w = 5.6 \pm 0.3 \times 10^5$ ,  $M_w/M_n = 3.7 \pm 0.2$ ,  $T_g = 38 \pm 1$  °C from a DSC equal area construction for  $\dot{T} = 10$  K/min) was investigated in the relevant frequency and temperature range with the aid of a dynamic analyzer RDA II and a dynamic stress analyzer DSR from Rheometrics Scientific, by a broad-band dielectric spectrometer from Novocontrol, and by specific heat spectroscopy according to Birge and Nagel<sup>5,6</sup> in a periodic calorimeter.<sup>7</sup> The relative mean uncertainty of the original shear data is not larger than 10%, corresponding to about the symbol size of Figure 2, below. Details of the sample preparation, the time-temperature program, and the comparability of the temperatures in the different devices will be published elsewhere.<sup>8</sup> The retardation spectrum  $L$  was calculated from the shear data by means of a nonlinear regularization program by Honerkamp and Weese.<sup>9</sup>

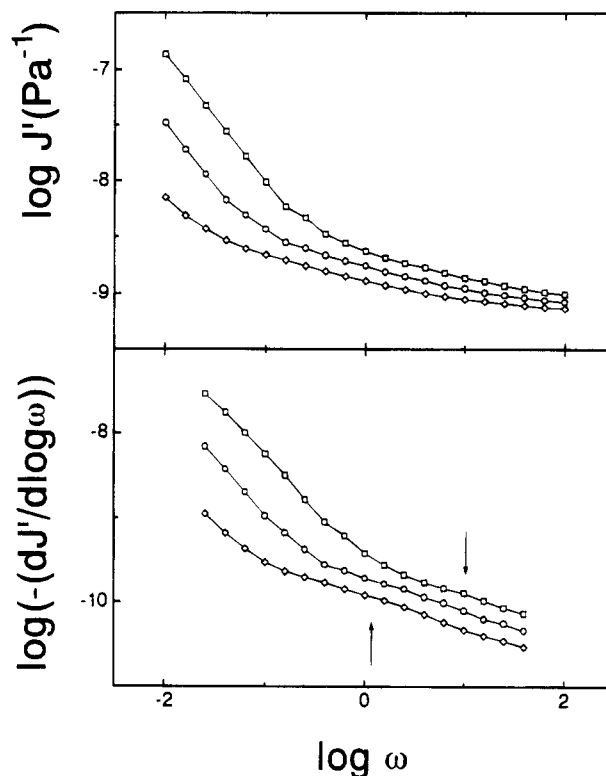
**Results and Discussion.** Figure 1 shows three isothermal shear retardation spectra calculated from shear frequency sweeps at the temperatures 41.5, 43.5, and 45.4 °C, with no temperature reduction. Each of the three curves demonstrates the slight shoulder that cannot, therefore, be caused by temperature-reduction errors.

The original data of the real part compliance ( $J'$ ) at these temperatures are shown in the upper part of Figure 2. The lower part of Figure 2 shows  $\log(-dJ'/d \log \omega)$ , smoothed with five-point splines. A slight indication of the shoulder can be detected also in this representation. [Similar results are obtained for repeated measurements, for a PVAC sample with higher water content, and for a commercial polystyrene sample. It seems that the occurrence of the shoulder does not depend on polydispersity.] Since the differentiation is a local procedure, the slight shoulder in  $L$  cannot be generated by the steep slope of the  $J'$  values in the main transition that could be, in principle, reflected by the nonlocality properties of the regularization program.

Figure 3 shows the sensitivity of this slight shoulder in a 56.6 °C master curve (from about 300 data) against a manipulated variation of the experimental data. The



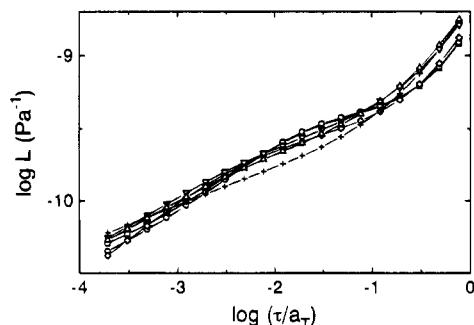
**Figure 1.** Shear retardation spectrum of PVAC: (□) 45.4, (○) 43.5, (◇) 41.5 °C. The arrows show the position of the slight shoulder. The  $\log$  symbol always means  $\log_{10}$  (logarithm on basis 10).



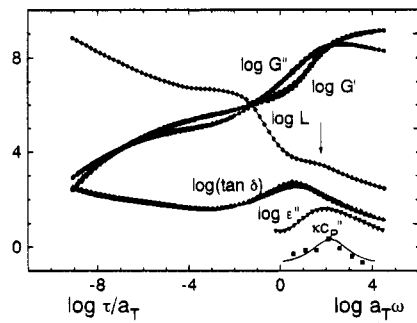
**Figure 2.** Original data of the real part of dynamic shear compliance,  $J'$  (upper part), from which the spectrum of Figure 1 was calculated. The lower part shows a smoothed differentiation of these curves.

shoulder resisted the following data manipulations: addition of random errors of  $\pm 10$  and  $\pm 20\%$  to each experimental point, a rarefaction of the data down to 10% (i.e., only any tenth point was used, in sum about 30 data), and a combination of rarefaction and  $\pm 10\%$  randomization. The shoulder is only lost by a combination of rarefaction plus the  $\pm 20\%$  randomization. The shoulder is also resistant to a data cutoff for  $\log \tau/a_T < -2.5$  (not shown in Figure 3). We conclude from this stability that the slight shoulder cannot be caused by experimental uncertainty.

Figure 4 shows the master curves for the real and imaginary part of the dynamic shear modulus,  $G^* = G' + i\omega G''$ , the shear loss factor,  $\tan \delta = G''/G'$ , and the shear retardation spectrum  $L$  reduced to  $T_0 = 56.6$  °C with a WLF equation,  $\log(f/\text{Hz}) = 10.9 - 451/(T/\text{K} - 275.6)$ ,  $f = \omega/2\pi$ . The  $\tau\omega$  conversion was again done by  $\omega\tau = 1$ . The frequency range of the shear data is  $10^{-2}$ – $10^2$  rad/s, and the temperature range, 41.5–148.5 °C.



**Figure 3.** Stability against manipulated data variation of a  $L$  master curve ( $T_0 = 56.6^\circ\text{C}$ ): (□) from the original master curve, (○) from the master curve with a random error of  $\pm 10\%$ , (◇) from the master curve with a random error of  $\pm 20\%$ , (Δ) from the master curve rarefied down to about 10% of the data, (▽) from the rarefied master curve with a random error of  $\pm 10\%$ , (+) from the rarefied master curve with a random error of  $\pm 20\%$ .



**Figure 4.** Comparison of shear modulus ( $\log G'$ ,  $\log G''$ ), shear loss factor ( $\log(\tan \delta)$ ), dielectric function ( $\log \epsilon''$ ), and heat spectroscopy ( $\kappa C''_P$ , linearly presented) with the slight shoulder in the shear retardation spectrum ( $\log L$ ). Arbitrary units, also for the dimensionless variables such as  $\tan \delta$  and  $\epsilon''$ , and  $\omega\tau = 1$ .

For comparison, the dielectric loss,  $\epsilon''$ , was measured at  $T = 58^\circ\text{C}$  and WLF corrected from this temperature to  $T_0$ . The imaginary output of heat spectroscopy was measured directly at  $T = 56.6^\circ\text{C}$ . Since the experi-

mental real part  $\kappa C'_P$  is more precise than the imaginary part  $\kappa C''_P$ , the  $\kappa C''_P$  curve was calculated from the real part by using the Kramers–Kronig relation via a fit with a Havriliak–Negami function.<sup>8</sup> Figure 4 demonstrates that the usual signals of a dynamic glass transition in equilibrium (no freezing-in) are about at the same position as Plazek's slight shoulder.

**Conclusions.** According to the fluctuation dissipation theorem, the natural frequencies (or times) of the spontaneous system fluctuations are identified<sup>3,4,10</sup> with the external frequencies (or relaxation times) at which the system can absorb energy. The slight  $L$  shoulder is, therefore, a direct consequence of the fluctuations which produce also the other (dielectric, caloric) signals of the proper glass transition. The large step of  $G'$ ,  $J'$ , or  $L$  in the main transition of polymers is therefore caused by other molecular modes (possibly confined flow and modified Rouse modes<sup>4</sup>). These modes are slower (and larger<sup>10</sup>) than the modes producing the proper glass transition. There is no contradiction of this thesis to the general relation  $G^*(\omega)J^*(\omega) = 1$ , with  $J^*$  the shear compliance, if the flank sensitivity of this relation is taken into account. The flank sensitivity means that very small (percent range) systematic variations of  $G^*(\omega)$  in the crossover from the main to the plateau zone can, just from the  $G^*J^* = 1$  relation, produce very large changes in the  $J^*$  values there.<sup>3</sup>

**Acknowledgment.** Support of the Deutsche Forschungsgemeinschaft (DFG) is gratefully acknowledged.

## References and Notes

- (1) Plazek, D. J. *Polym. J. Jpn.* **1980**, *12*, 43.
- (2) Plazek, D. L.; Plazek, D. J. *Macromolecules* **1983**, *16*, 1469.
- (3) Donth, E.; Schneider, K. *Acta Polym.* **1985**, *36*, 213.
- (4) Donth, E.; Schneider, K. *Acta Polym.* **1985**, *36*, 273.
- (5) Birge, N. O.; Nagel, S. R. *Phys. Rev. Lett.* **1985**, *54*, 2674.
- (6) Birge, N. O.; Nagel, S. R. *Phys. Rev. B* **1986**, *34*, 1631.
- (7) Korus, J.; et al., to be published.
- (8) Beiner, M.; et al., to be published.
- (9) Honerkamp, J.; Weese, J. *Rheol. Acta* **1993**, *32*, 63.
- (10) Donth, E. *Relaxation and Thermodynamics in Polymers. Glass Transition*; Akademie-Verlag: Berlin, 1992.

MA950401C